# BILATERAL GRADUAL SEMANTICS FOR WEIGHTED ARGUMENTATION



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#### OVERVIEW

#### Bilateral gradual semantics for weighted argumentation

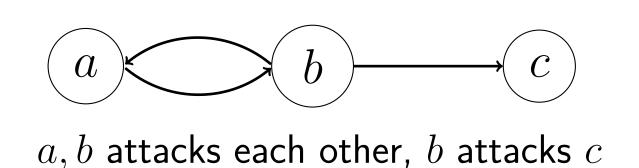
- Evaluate argument strength through a **bilateral** perspective
- Propose desirable principles for our semantics
- Provide three **well-behaved** semantics

#### ARGUMENTATION GRAPH

**Abstract argumentation** is a well-studied model for evaluating arguments in conflict situations.

An **Argumentation Graph** is a pair  $\langle A, \mathcal{R} \rangle$ , where

- $\bullet \mathcal{A}$  is a finite set of arguments,
- $\mathcal{R} \subseteq \mathcal{A} \times \mathcal{A}$  is an attack relation between arguments.



#### Extension Semantics:

- Select sets of arguments with desirable principles
- Accepts  $\{a, c\}$  or  $\{b\}$  but not  $\{a, b, c\}$

## WEIGHTED ARGUMENTATION GRAPH

A Weighted Argumentation Graph is a triple  $G = \langle A, w, \mathcal{R} \rangle$ , where

- $\bullet \mathcal{A}$  is a finite set of arguments,
- w is a weighting function from  $\mathcal{A}$  to [0,1],
- $\mathcal{R} \subseteq \mathcal{A} \times \mathcal{A}$  is an attack relation between arguments.

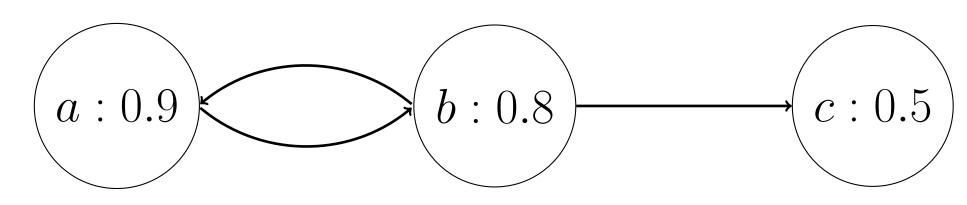
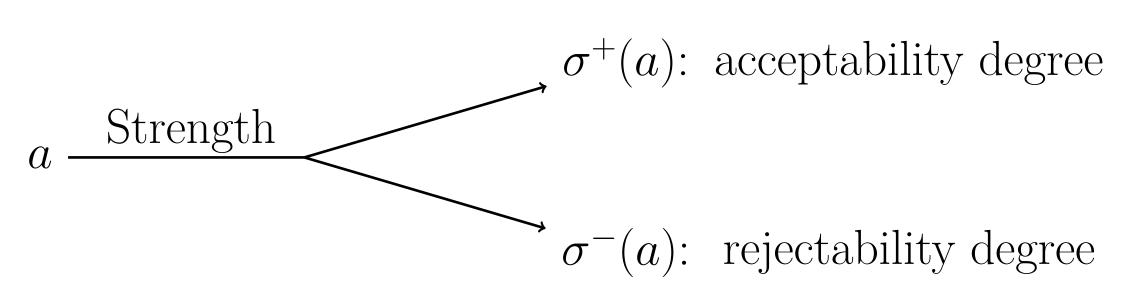


Figure. Arguments with basic weights

Gradual semantics assign each argument an acceptability degree, representing its strength, along with a set of desirable principles.

#### BILATERAL GRADUAL SEMANTICS

Motivation: Argument strength of *positivity* and *negativity* should be separately considered in the evaluative process.



A Bilateral Gradual Semantics (BGS)  $\mathcal{S}$  transforms any WAG  $\mathbf{G} = \langle \mathcal{A}, w, \mathcal{R} \rangle$  to a function  $Deg_{\mathbf{G}}^{\mathcal{S}} \colon \mathcal{A} \to [0, 1] \times [0, 1]$ . For any  $a \in \mathcal{A}$ ,  $Deg_{\mathbf{G}}^{\mathcal{S}}(a) = (\sigma_{\mathbf{G}}^{+}(a), \sigma_{\mathbf{G}}^{-}(a))$  where  $\sigma_{\mathbf{G}}^{+}(a)$  and  $\sigma_{\mathbf{G}}^{-}(a)$  represent the acceptability and rejectability degree of a respectively.

#### Non-reciprocity of BGS

| Degree        | Source of Strength                  |
|---------------|-------------------------------------|
|               | • basic weight                      |
| acceptability | • acceptability degree of attackers |
|               | • rejectability degree of attackers |
| rejectability | • acceptability degree of attackers |

### Principles for BGS

| Dagie itema | Anonymity          | Independence              | Directionality  |  |
|-------------|--------------------|---------------------------|-----------------|--|
| Basic items | Equivalence        | Resilience                | Proportionality |  |
| Symmetric   | A-Neutrality       | A-Weakening               | A-Counting      |  |
|             | R-Neutrality       | R-Strengthening           | R-Counting      |  |
|             | A-Reinforcement    | A-Weakening Soundness     | A-Maximality    |  |
|             | R-Reinforcement    | R-Strengthening Soundness | R-Minimality    |  |
| Defense     | Weakened Defense   | Strict Weakened Defense   |                 |  |
| Strategies  | Quality Precedence | Cardinality Precedence    | Compensation    |  |

- A-Counting: acceptability degree decreases as attackers increase
- R-Counting: rejectability degree increases as attackers increase
- Quality Precedence (QP) prioritizes the quality of attackers.
- Cardinality Precedence (CP) prioritizes the quantity of attackers.
- Compensation considers both the quantity and quality of attackers.

#### FOUNDATIONS FOR SEMANTICS

| Quality Precedence     | $f^{i}(a) = \frac{w(a)}{1 + \max_{b \in Att(a)} \frac{f^{i-1}(b)}{1 + g^{i-1}(b)}}$                                                                              |
|------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Iterative Function     | $g^{i}(a) = \frac{\max_{b \in Att(a)} f^{i-1}(b)}{1 + \max_{b \in Att(a)} f^{i-1}(b)}$                                                                           |
| Cardinality Precedence | $f^{i}(a) = \frac{w(a)}{1 +  Att^{*}(a)  + \frac{1}{n} \cdot \sum_{b \in Att^{*}(a)} \frac{f^{i-1}(b)}{1 + g^{i-1}(b)}}$                                         |
| Iterative Function     | $g^{i}(a) = \frac{ Att^{*}(a)  + \frac{1}{n} \cdot \sum_{b \in Att^{*}(a)} f^{i-1}(b)}{1 +  Att^{*}(a)  + \frac{1}{n} \cdot \sum_{b \in Att^{*}(a)} f^{i-1}(b)}$ |
| Compensation           | $f^{i}(a) = \frac{w(a)}{1 +  Att^{*}(a)  + \sum_{b \in Att^{*}(a)} \frac{f^{i-1}(b)}{1 + g^{i-1}(b)}}$                                                           |
| Iterative Function     | $g^{i}(a) = \frac{ Att^{*}(a)  + \sum_{b \in Att^{*}(a)} f^{i-1}(b)}{1 +  Att^{*}(a)  + \sum_{b \in Att^{*}(a)} f^{i-1}(b)}$                                     |

**Theorem**: All iterative functions converge as i approaches  $\infty$ .

#### SEMANTICS

Three semantics for Quality Precedence, Cardinality Precedence, and Compensation, respectively.

- AR-max-based Semantics is defined as the limit of Quality Precedence Iterative Function.
- AR-card-based Semantics is defined as the limit of Cardinality Precedence Iterative Function.
- AR-hybrid-based Semantics is defined as the limit of Compensation Iterative Function.

|                           | ARM      | ARC      | ARH          |
|---------------------------|----------|----------|--------------|
| Anonymity                 | <b>√</b> | <b>√</b> | <b>√</b>     |
| Independence              | <b>√</b> | <b>√</b> | <b>√</b>     |
| Directionality            | <b>√</b> | <b>√</b> | <b>√</b>     |
| Equivalence               | <b>√</b> | <b>√</b> | <b>√</b>     |
| Resilience                | <b>√</b> | <b>√</b> | <b>√</b>     |
| Proportionality           | <b>√</b> | <b>√</b> | <b>√</b>     |
| A-Neutrality              | <b>√</b> | <b>√</b> | <b>√</b>     |
| R-Neutrality              | <b>√</b> | <b>√</b> | <b>√</b>     |
| A-Maximality              | <b>√</b> | <b>√</b> | <b>√</b>     |
| R-Minimality              | <b>√</b> | <b>√</b> | <b>√</b>     |
| A-Weakening               | <b>√</b> | <b>√</b> | $\checkmark$ |
| R-Strengthening           | <b>√</b> | <b>√</b> | <b>√</b>     |
| A-Weakening soundness     | <b>√</b> | <b>√</b> | <b>√</b>     |
| R-Strengthening soundness | <b>√</b> | <b>√</b> | <b>√</b>     |
| A-Counting                | _        | <b>√</b> | <b>√</b>     |
| R-Counting                | _        | <b>√</b> | <b>√</b>     |
| A-Reinforcement           | _        | <b>√</b> | <b>√</b>     |
| R-Reinforcement           | _        | <b>√</b> | <b>√</b>     |
| Weakened Defense          | <b>√</b> | <b>√</b> | <b>√</b>     |
| Strict Weakened Defense   | _        | <b>√</b> | <b>√</b>     |
| Quality Precedence        | <b>√</b> | _        | _            |
| Cardinality Precedence    | _        | <b>√</b> | _            |
| Compensation              | _        | _        | <b>√</b>     |

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